

Topic : Mathematical Tools

Type of Questions

Type of Questions	M.M., Min.
Single choice Objective ('-1' negative marking) Q.1 to Q.4	(3 marks, 3 min.) [12, 12]
Subjective Questions ('-1' negative marking) Q.5 to Q. 6	(4 marks, 5 min.) [8, 10]
Comprehension ('-1' negative marking) Q.7 to Q.9	(3 marks, 3 min.) [9, 9]

- Maximum value of $f(x) = \sin x + \cos x$ is :
(A) 1 (B) 2 (C) $\frac{1}{\sqrt{2}}$ (D) $\sqrt{2}$
- The displacement of a body at any time t after starting is given by $s = 15t - 0.4t^2$. The velocity of the body will be 7 ms^{-1} after time :
(A) 20 s (B) 15 s (C) 10 s (D) 5 s
- For the previous question, the acceleration of the particle at any time t is :
(A) -0.8 m/s^2 (B) 0.8 m/s^2 (C) -0.6 m/s^2 (D) 0.5 m/s^2
- A particle is moving in a straight line. Its displacement at time t is given by s (in m) = $-4t^2 + 2t$, then its velocity and acceleration at time $t = \frac{1}{2}$ second are
(A) $-2 \text{ m/s}, -8 \text{ m/s}^2$ (B) $2 \text{ m/s}, 6 \text{ m/s}^2$ (C) $-2 \text{ m/s}, 8 \text{ m/s}^2$ (D) $2 \text{ m/s}, 8 \text{ m/s}^2$
- A stone thrown upwards from ground level, has its equation of height $h = 490t - 4.9t^2$ where 'h' is in metres and t is in seconds respectively. What is the maximum height reached by it ?
- If $\int (x+1)dy$

COMPREHENSION

If a man has a velocity varying with time given as $v = 3t^2$, v is in m/s and t in sec then :



- Find out the velocity of the man after 3 sec.
(A) 18 m/s (B) 9 m/s (C) 27 m/s (D) 36 m/s
- Find out his displacement after 2 seconds of his start :
(A) 10 m (B) 6 m (C) 12 m (D) 8 m
- Find out his acceleration after 3 seconds :
(A) 9 m/s^2 (B) 18 m/s^2 (C) 12 m/s^2 (D) 6 m/s^2

Answers Key

DPP NO. - 5

1. (D) 2. (C) 3. (A) 4. (A)
5. 12250 m 6. $4x^3 + 6x^2 + C$
7. (C) 8. (D) 9. (B)

Hint & Solutions

DPP NO. - 5

1. $y = f(x) = \sin x + \cos x$

$$\frac{dy}{dx} = \cos x - \sin x$$

$$\frac{dy}{dx} = 0, \sin x = \cos x, \tan x = 1$$

$$x = 45^\circ$$

$$y = \sin 45^\circ + \cos 45^\circ$$

$$= \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}}$$

$$= \frac{2}{\sqrt{2}} = \sqrt{2}$$

Alter : $f(x) = \sqrt{2} \sin(x + \frac{\pi}{4})$

$$f(x)_{\max} = \sqrt{2}$$

2. (C*) 10 s

3. $\frac{ds}{dt} = 15 - 0.8t = 7 = v$

; $8 = 0.8t$; $t = 10$ second.

$$a = \frac{d^2s}{dt^2} = -0.8 \text{ m/s}^2$$

4. (A*) -2 m/s , -8 m/s^2



5. $\frac{ds}{dt} = 490 - 9.8t = 0 \quad t = \frac{490}{9.8} = 50 \text{ second.}$

$$S_{\max} = 490 \times 50 - 4.9 \times 2500 = 12250 \text{ m}$$

6. $dy = 12x dx \quad \int (x+1)(12x) dx = 4x^3 + 6x^2 + C$

7. $v = 3t^2$

$$v = 3(3)^2 = 27 \text{ m/s}$$

8. $\int_0^s dS = \int_0^2 3t^2 dt$

$$S = \left[t^3 \right]_0^2 = 8$$

9. $f = \frac{dv}{dt} = 6t$

$$f = 6 \times 3 = 18 \text{ m/s}^2$$